PAPER NAME AUTHOR

On the locating chromatic number of bar bell shadow path graphs

WORD COUNT CHARACTER COUNT

3673 Words 13887 Characters

PAGE COUNT FILE SIZE

12 Pages 322.6KB

SUBMISSION DATE REPORT DATE

Jan 23, 2023 11:04 AM GMT+7 Jan 23, 2023 11:04 AM GMT+7

Asmiati

14% Overall Similarity

The combined total of all matches, including overlapping sources, for each database.

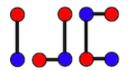
- 9% Internet database
- · Crossref database
- 8% Submitted Works database

- 11% Publications database
- · Crossref Posted Content database

Excluded from Similarity Report

- · Bibliographic material
- Cited material
- · Manually excluded sources

- Ouoted material
- Small Matches (Less then 10 words)



INDONESIAN JOURNAL OF COMBINATORICS

On the locating chromatic number of barbell shadow path graphs

Asmiati^a, Maharani Damayanti^a, Lyra Yulianti^b

asmiati.1976@fmipa.unila.ac.id

Abstract

The locating chromatic number was introduced by Chartrand in 2002. The locating chromatic number of a graph is a combined concept between the coloring and partition dimension of a graph. The locating chromatic number of a graph is defined as the cardinality of the minimum color classes of the graph. In this paper, we discuss about the locating chromatic number of shadow path graphs and barbell graph containing shadow graph.

Keywords: the locating-chromatic number, shadow path graph, barbell graph

Mathematics Subject Classification: 05C12, 05C15

DOI: 10.19184/ijc.2021.5.2.4

1. Introduction

The locating chromatic number of a graph was introduced by Chatrand et al.[6] by combining two concepts in graph theory, which are vertex coloring and partition dimension of a graph. Let G = (V, E) be a connected graph. A k-coloring of G is a function $c: V(G) \longrightarrow \{1, 2, \cdots, k\}$, where $c(u) \neq c(v)$ for any two adjacent vertices u and v in G. Thus, the coloring c induces a partition Π of V(G) into k color classes (independent sets) C_1, C_2, \cdots, C_k , where C_i is the set of all vertices colored by the color i for $1 \leq i \leq k$. The color code $c_{\Pi}(v)$ of a vertex v in G is defined

24—Received: 12 February 2021, Revised: 7 July 2021, Accepted: 25 September 2021.

^aDepartment of Mathematics, Faculty of Mathematics and Natural Sciences, Universitas Lampung,

Jl. Sumantri Projonegoro No 1, Bandar Lampung, Indonesia

^bDepartment of Mathematics, Faculty of Mathematics and Natural Sciences, Universitas Andalas, Kampus UNAND Limau Manis, Padang, Indonesia

as the k-ordinate $(d(v, C_1), d(v, C_2), \cdots, d(v, C_k))$, where $d(v, C_i) = \min\{d(v, x); x \in C_i\}$ for $1 \le i \le k$. The k-coloring c of c such that all vertices have different color codes is called a locating coloring of c. The locating chromatic number of c, denoted by c is the minimum c such that c has a locating coloring.

The following two theorems are useful to determine the lower bound of the locating chromatic of a graph. The set of neighbors of a vertex q in G, denoted by N(q).

Theorem 1.1. (see [6]). Let c be a locating coloring in a connected graph G. If x and y are distinct vertices of G such that d(p, w) = d(q, w) for all $w \in V(G) - \{p, q\}$, then $c(p) \neq c(q)$. In particular, if p and q are non-adjacent vertices such that $N(p) \neq N(q)$, then $c(p) \neq c(q)$.

Theorem 1.2. (see [6]). The locating chromatic number of a cycle graph $C_n (n \ge 3)$ is 3 for odd n and 4 for even n.

The locating chromatic number of a graph is an interesting topic to study because there is no general algorithm for determining the locating chromatic number of any graphs and there are only a few results related to determining of the locating chromatic number of some graphs. Chartrand $et\ al.$ [6] determined all graphs of order n with locating number n, namely a complete multipartite graph of n vertices. Moreover, Chartrand $et\ al.$ [7] provided a tree construction of n vertices, $n\geq 5$, with locating chromatic number varying from 3 to n, except for (n-1). Next, Asmiati $et\ al.$ [1] obtained the locating chromatic number of amalgamation of stars and non-homogeneous caterpillars and firecracker graphs [2]. In [5] Welyyanti $et\ al.$ determined the locating chromatic number of homogeneous lobster. Next, Sofyan $et\ al.$ [4] determined the locating chromatic number of homogeneous lobster. Recently, Ghanem $et\ al.$ [8] found the locating chromatic number of powers of the path and cycles.

Let P_n be a path with $V(P_n)=\{x_i\mid 1\leq i\leq n\}$ and $E(P_n)=\{x_ix_{i+1}\mid 1\leq i\leq n-1\}$. The shadow path graph $D_2(P_n)$ is a graph with the vertex set $\{u_i,v_i\mid 1\leq i\leq n\}$ where $u_iu_j\in E(D_2(P_n))$ if and only if $x_ix_j\in E(P_n)$ and $u_iv_j\in E(D_2(P_n))$ if and only if $x_ix_j\in E(P_n)$. A barbell graph containing shadow path graph, denoted by $B_{D_2(P_n)}$ is obtained by copying a shadow path graph (namely, $D_2'(P_n)$) and connecting the two graphs with a bridge. We assume that $\{u_i',v_i'\mid 1\leq i\leq n\}$ is a vertex set of $D_2'(P_n)$ and a bridge in $B_{D_2(P_n)}$ connecting $\{u_{n+1}'v_{$

Motivated by the result of Asmiati *et al.* [3] about the determination of the locating chromatic number of certain barbell graphs, in this paper we determine the locating chromatic number of shadow path graphs and barbell graph containing shadow path for $n \ge 3$.

Main Results

The following theorem gives the locating chromatic number for shadow path graph $D_2(P_n)$ for $n \geq 3$.

Lemma 2.1. Let c be a locating-chromatic number for shadow path graph $D_2(P_n)$, with $u_i \in P_i^1$ and $v_i \in P_i^2$. Then $c(u_i) \neq c(v_i)$.

Proof. On the shadow path graph $D_2(P_n)$, we can see that $d(u_i, x) = d(v_i, x)$, $i \in [1, n-1]$ for every $x \in ((D_2(P_n)) \setminus \{u_i, v_i\})$. By Theorem 1.1, we have $c(u_i) \neq c(v_i)$.

Theorem 2.1. The locating chromatic number of a shadow path graph for $n \geq 3$, $D_2(P_n)$ is 6.

Proof. First, we determine the lower bound for the locating-chromatic number of shadow path graph $D_2(P_n)$ for $n \geq 3$. The Shadow path graph $D_2(P_n)$ for $n \geq 3$ consists of minimal two cycles C_4 . Pick the first cycle C_4 , then by Theorem 1.2, we could assign 4 colors, $\{1, 2, 3, 4\}$ to the first cycle's vertices. Next, in the second C_4 , we have two vertices, which intersect with two vertices in the first C_4 . By Lemma 2.1, we must assign two different colors to the remaining vertices of the second C_4 . Therefore, we have $\chi_L(G) \geq 6$.

Next, we determine the upper bound of the locating chromatic number of the shadow path graph for $n \geq 3$. Let c be a coloring using 6 colors as follow:

$$c(u_i) = \begin{cases} 1, & \text{for } i = 1, \\ 2, & \text{for } i = 2n, n \ge 1, \\ 3, & \text{for } i = 2n + 1, n \ge 1, \end{cases}$$

$$c(v_i) = \begin{cases} 4, & \text{for } i = 1, \\ 5, & \text{for } i = 2n, n \ge 1, \\ 6, & \text{for } i = 2n + 1, n \ge 1. \end{cases}$$

The color codes of $D_2(P_n)$ are :

$$c_{\pi}(u_i) = \begin{cases} 0, & \text{for } i = 2n+1, n \geq 1. \\ 0, & \text{for } 1^{st} \text{ ordinate, } i \geq 1, \\ & \text{for } 4^{th} \text{ ordinate, } i \geq 2, \\ 0, & \text{for } 2^{nd} \text{ ordinate, even i }, 2 \leq i \leq n, \\ & \text{for } 3^{rd} \text{ ordinate, odd i }, 3 \leq i \leq n, \\ & \text{for } 5^{th} \text{ ordinate, even i }, 2 \leq i \leq n, \\ & \text{for } 6^{th} \text{ ordinate, odd i }, 1 \leq i \leq n, \\ & \text{for } 3^{rd} \text{ ordinate, } i = 1, \\ & \text{for } 4^{th} \text{ ordinate, } i \geq 1, \\ 1, & \text{otherwise,} \end{cases}$$

$$\begin{cases} i-1, & \text{for } 1^{st} \text{ ordinate, } i \geq 2, \\ & \text{for } 4^{th} \text{ ordinate, } i \geq 1, \\ 0, & \text{for } 5^{nd} \text{ ordinate, even i }, 2 \leq i \leq n, \\ & \text{for } 6^{th} \text{ ordinate, odd i }, 3 \leq i \leq n, \\ & \text{for } 3^{rd} \text{ ordinate, odd i }, 3 \leq i \leq n, \\ & \text{for } 3^{rd} \text{ ordinate, odd i }, 3 \leq i \leq n, \\ & \text{for } 1^{st} \text{ ordinate, odd i }, 3 \leq i \leq n, \\ & \text{for } 1^{st} \text{ ordinate, } i = 1, \\ & \text{for } 6^{th} \text{ ordinate, } i = 1, \\ & \text{for } 6^{th} \text{ ordinate, } i = 1, \\ & \text{for } 6^{th} \text{ ordinate, } i = 1, \\ & \text{totherwise.} \end{cases}$$

Since all vertices in $D_2(P_n)$ for $n \ge 3$ have distinct color codes, then c is a locating coloring using 6 colors. As a result $\chi_L D_2(P_n) \leq 6$. Thus $\chi_L D_2(P_n) = 6$.

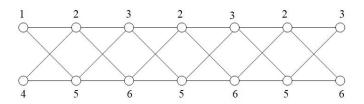


Figure 1. A minimum locating coloring of $D_2(P_7)$.

Theorem 2.2. The locating chromatic number of a barbell graph containing shadow path for $n \geq 3$ is 6.

Proof. First, we determine the lower bound of $\chi_L B_{D_2(P_n)}$ for $n \geq 3$. Since the barbell graph $B_{D_2(P_n)}$ containing $D_2(P_n)$, then by Theorem 2.3 we have $\chi_L(B_{D_2(P_n)}) \geq 6$. To prove the upper bound, consider the following three cases.

CASE 1 (n = 3). Let c be a locating coloring using 6 colors as follows:

$$c(u_i) = \begin{cases} 1, & \text{for } i = 2, \\ 2, & \text{for } i = 1, \\ 3, & \text{for } i = 3, \end{cases}$$

$$c(u_i') = \begin{cases} 4, & \text{for } i = 2, \\ 5, & \text{for } i = 1, \\ 6, & \text{for } i = 3, \end{cases}$$

$$c(v_i) = \begin{cases} 1, & \text{for } i = 1, \\ 5, & \text{for } i = 1, \\ 6, & \text{for } i = 2, \end{cases}$$

$$c(v_i') = \begin{cases} 2, & \text{for } i = 1, \\ 3, & \text{for } i = 3, \\ 4, & \text{for } i = 2. \end{cases}$$

$$c(v_i') = \begin{cases} 2, & \text{for } i = 1, \\ 3, & \text{for } i = 3, \\ 4, & \text{for } i = 2. \end{cases}$$

$$c(v_i') = \begin{cases} 1, & \text{for } i = 1, \\ 2, & \text{for } i = 1, \\ 3, & \text{for } i = 2. \end{cases}$$

$$c(v_i') = \begin{cases} 1, & \text{for } i = 1, \\ 2, & \text{for } i = 1, \\ 3, & \text{for } i = 2. \end{cases}$$

$$c(v_i') = \begin{cases} 1, & \text{for } i = 1, \\ 2, & \text{for } i = 1, \\ 3, & \text{for } i = 3, \\ 4, & \text{for } i = 2. \end{cases}$$

$$c(v_i') = \begin{cases} 1, & \text{for } i = 1, \\ 2, & \text{for } i = 1, \\ 3, & \text{for } i = 3, \\ 4, & \text{for } i = 2. \end{cases}$$

$$c(v_i') = \begin{cases} 1, & \text{for } i = 1, \\ 3, & \text{for } i = 3, \\ 4, & \text{for } i = 2. \end{cases}$$

$$c(v_i') = \begin{cases} 1, & \text{for } i = 1, \\ 3, & \text{for } i = 3, \\ 4, & \text{for } i = 2. \end{cases}$$

$$c(v_i') = \begin{cases} 1, & \text{for } i = 1, \\ 3, & \text{for } i = 3, \\ 4, & \text{for } i = 2. \end{cases}$$

The color codes of $B_{D_2(P_3)}$ are

$$c_{\pi}(u_{i}) = \begin{cases} 0, & \text{for } 1^{st} \text{ ordinate, } i = 2, \\ & \text{for } 2^{nd} \text{ ordinate, } i = 1, \\ & \text{for } 3^{rd} \text{ ordinate, } i = 3, \end{cases}$$

$$2, & \text{for } 3^{th} \text{ ordinate, } i = 1, \\ & \text{for } 4^{th} \text{ ordinate, } i = 2, \\ & \text{for } 2^{nd} \text{ ordinate, } i = 3, \\ & \text{for } 5^{th} \text{ and } 6^{th} \text{ ordinate, } i = 1 \text{ and } 3, \end{cases}$$

$$1, & \text{otherwise,}$$

$$c_{\pi}(u_i') = \begin{cases} 0, & \text{for } 5^{th} \text{ ordinate, } i=1, \\ & \text{for } 4^{th} \text{ ordinate, } i=2, \\ & \text{for } 6^{th} \text{ ordinate, } i=3, \end{cases} \\ 2, & \text{for } 6^{th} \text{ ordinate, } i=1, \\ & \text{for } 1^{nd} \text{ ordinate, } i=2, \\ & \text{for } 5^{th} \text{ ordinate, } i=3, \\ & \text{for } 2^{nd} \text{ and } 3^{rd} \text{ ordinate, } i=1 \text{ and } 3, \end{cases} \\ 1, & \text{otherwise,} \end{cases}$$

$$c_{\pi}(v_i) = \begin{cases} 0, & \text{for } 1^{st} \text{ ordinate, } i=1, \\ & \text{for } 6^{th} \text{ ordinate, } i=2, \\ & \text{for } 5^{th} \text{ ordinate, } i=3, \end{cases} \\ 2, & \text{for } 5^{th} \text{ ordinate, } i=3, \\ & \text{for } 1^{st} \text{ ordinate, } i=1, \\ & \text{for } 1^{st} \text{ ordinate, } i=1 \text{ and } 3, \end{cases} \\ 1, & \text{otherwise,} \end{cases}$$

$$c_{\pi}(v_i') = \begin{cases} 0, & \text{for } 2^{nd} \text{ ordinate, } i=1, \\ & \text{for } 3^{rd} \text{ ordinate, } i=2, \\ & \text{for } 3^{rd} \text{ ordinate, } i=2, \\ & \text{for } 3^{rd} \text{ ordinate, } i=3, \end{cases} \\ 2, & \text{for } 1^{st} \text{ ordinate, } i=2, \\ & \text{for } 2^{nd} \text{ ordinate, } i=3, \end{cases} \\ 2, & \text{for } 1^{st} \text{ ordinate, } i=3, \end{cases}$$

$$1, & \text{otherwise.} \end{cases}$$
all vertices in $B_{D^n(P^n)}$ have distinct color codes, then c is a locating coloring and all vertices in C and C a

Since all vertices in $B_{D_2(P_3)}$ have distinct color codes, then c is a locating coloring using 6 colors. As a result $\chi_L B_{D_2(P_3)} \leq 6$. Thus $\chi_L B_{D_2(P_3)} = 6$.

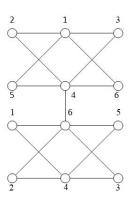


Figure 2. A minimum locating coloring of $B_{D_2(P_3)}$.

CASE 2 (n odd). Let a be a locating coloring using 6 colors as follows:

$$c(u_i) = \begin{cases} 1, & \text{for } i = \frac{n+1}{2}, \\ 2, & \text{for odd } i; i < \frac{n+1}{2}, \\ n = 4j+3, j \ge 1 \text{ and } i > \frac{n+1}{2}, \\ n = 4j+1, j \ge 1 \text{ and } i > \frac{n+1}{2}, \\ n = 4j+3, j \ge 1, \\ 3, & \text{for even } i; i < \frac{n+1}{2}, \\ n = 4j+1, j \ge 1 \text{ and } i > \frac{n+1}{2}, \\ n = 4j+3, j \ge 1, \\ 3, & \text{for odd } i; i < \frac{n+1}{2}, \\ n = 4j+1, j \ge 1 \text{ and } i > \frac{n+1}{2}, \\ n = 4j+3, j \ge 1, \\ 4, & \text{for } i = \frac{n+1}{2}, \\ 5, & \text{for odd } i; i < \frac{n+1}{2}, \\ n = 4j+3, j \ge 1 \text{ and } i > \frac{n+1}{2}, \\ n = 4j+1, j \ge 1, \\ 6, & \text{for even } 1; i < \frac{n+1}{2}, \\ n = 4j+1, j \ge 1 \text{ and } i > \frac{n+1}{2}, \\ n = 4j+3, j \ge 1, \\ 6, & \text{for odd } i; i < \frac{n+1}{2}, \\ n = 4j+3, j \ge 1 \text{ and } i > \frac{n+1}{2}, \\ n = 4j+1, j \ge 1, \\ n = 4j+1, j$$

$$c_{\pi}(u_i) = \begin{cases} (\frac{i+1}{2}) - i, & \text{for } 1^{st} \text{ ordinate, } i \leq \frac{n+1}{2}, \\ i - (\frac{n+1}{2}), & \text{for } 1^{st} \text{ ordinate, } i < \frac{n+1}{2}, \\ i - (\frac{n+1}{2}), & \text{for } 1^{st} \text{ ordinate, } i > \frac{n+1}{2}, \\ for 4^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 5^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 4^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 4^{th} \text{ ordinate, } i \leq \frac{n+1}{2}, \\ i - (\frac{n+1}{2}), & \text{for } 1^{st} \text{ ordinate, } i > \frac{n+1}{2}, \\ for 5^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ for 5^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ for 5^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ for 5^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ for 5^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 5^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 5^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 6^{th} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i > \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordinate, } \cot i, i < \frac{n+1}{2}, \\ for 3^{rd} \text{ ordin$$

$$c_{\pi}(v_i) = \begin{cases} \frac{(n+1)}{2} - i, & \text{for } 4^{th} \text{ ordinate, } i < \frac{n+1}{2}, \\ & \text{for } 6^{th} \text{ ordinate, } i \leq \frac{n+1}{2}, \\ & \text{i.} - (\frac{n+1}{2}), & \text{for } 4^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ & \text{for } 6^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ & \text{for } 6^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ & \text{for } 1^{st} \text{ ordinate, odd } i, i < \frac{n+1}{2}, \\ & \text{for } 1^{st} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 5^{th} \text{ ordinate, even } i, i < \frac{n+1}{2}, \\ & \text{for } 5^{th} \text{ ordinate, even } i, i < \frac{n+1}{2}, \\ & \text{for } 2^{nd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i < \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i < \frac{n+1}{2}, \\ & \text{for } 1^{st} \text{ ordinate, } i = \frac{n+1}{2}, \\ & \text{otherwise,} \end{cases}$$

$$\begin{cases} (\frac{n+1}{2}) - i, & \text{for } 4^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ & \text{for } 6^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ & \text{for } 6^{th} \text{ ordinate, } i > \frac{n+1}{2}, \\ & \text{for } 2^{nd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, odd } i, i < \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, odd } i, i < \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, odd } i, i < \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 1^{st} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 1^{st} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, even } i, i > \frac{n+1}{2}, \\ & \text{for } 3^{rd} \text{ ordinate, e$$

Since all vertices in $B_{D_2(P_n)}$, n > 3 for odd n have distinct color codes, then c is a locating coloring using 6 colors. As a result $\chi_L B_{D_2(P_n)} \leq 6$. Thus $\chi_L B_{D_2(P_n)} = 6$.

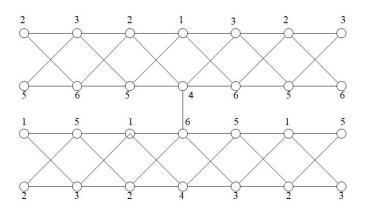


Figure 3. A minimum locating coloring of $B_{D_2(P_7)}$

CASE 3 (n even). Let c be a locating coloring using 6 colors as follows:

$$c(u_i) = \begin{cases} 1, & \text{for } i = \frac{n}{2}, \\ 2, & \text{for odd } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j + 2, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j + 2, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ 3, & \text{for odd } \mathbf{i}; i < \frac{n}{2}, \ n = 4j + 2, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j + 2, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j + 2, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j + 2, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j + 2, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j + 2, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n = 4j, j \geq 1, \\ \text{for even } \mathbf{i}; i < \frac{n}{2}, \ n = 4j, j \geq 1 \ \text{and } i > \frac{n}{2}, \ n$$

$$c_{\pi}(v_i) = \begin{cases} (\frac{n}{2}) & \mathbf{q} \\ i & \text{for } 4^{th} \text{ ordinate, } i < \frac{n}{2}, \\ i & \mathbf{q} \\ i &$$

Since all vertices in $B_{D_2(P_n)}$, $n \geq 3$ for even n have distinct color codes, then c is a locating coloring using 6 colors. As a result $\chi_L B_{D_2(P_n)} \leq 6$. Thus $\chi_L B_{D_2(P_n)} = 6$.

3. Concluding Remarks

The locating chromatic number of a shadow path graphs and the barbell graph containing a shadow path graph is similar, which is 6.

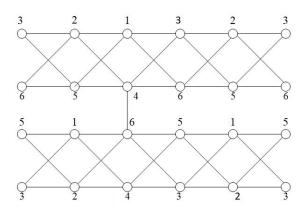


Figure 4. A minimum locating coloring of $B_{D_2(P_6)}$

References

- [1] Asmiati, H. Assiyatun and E.T. Baskoro, Locating-chromatic number of amalgamation of stars, *ITB J. of Sci.* **43**(1) (2011), 1–8.
- [2] Asmiati, On the locating-chromatic number of non-homogeneous caterpillars and firecracker graphs, *Far East J. Math. Sci.* **100**(8) (2016), 1305–1316.
- [3] Asmiati, I. Ketut S. G. Y. and L. Yulianti, On the locating chromatic number of certain barbell graphs, *Int. J. Math. Math. Sci.* **2018** (2018), 1–5.
- [4] D. K. Sofyan, E. T. Baskoro, and H. Assiyatun, On the locating chromatic number of homogeneous lobster, *AKCE Int. J. Graphs Comb.* **10**(3) (2013), 245–252.
- [5] D. Welyyanti, E. T. Baskoro, R. Simanjuntak and S. Uttunggadewa, On the locating chromatic number of complete n-ary tree, *AKCE Int. J. Graphs Comb.* **10**(3) (2013), 309–315.
- [6] G. Chartrand, D. Erwin, M. A. Henning, P. J. Slater, and P. Zhang, The locating-chromatic number of a graph, *Bull. Inst. Combin. Appl.* **36** (2002), 89–101.
- [7] G. Chartrand, D. Erwin, M. A. Henning, P. J. Slater, and P. Zhang, Graphs of order n-1, *Discrete Math.* **269**(1-3) (2003), 65–79.
- [8] M. Ghanem, H. Al-Ezeh, A. Dabour, Locating chromatic number of powers of path and cycles, *Symmetry* **11**(389) (2019), 2–8, https://doi.org/10.3390/sym11030389

14% Overall Similarity

Top sources found in the following databases:

- 9% Internet database
- Crossref database
- 8% Submitted Works database

- 11% Publications database
- Crossref Posted Content database

TOP SOURCES

The sources with the highest number of matches within the submission. Overlapping sources will not be displayed.

Eiji Kurozumi. "THE LIMITING PROPERTIES OF THE CANOVA AND HAN. Crossref	" 1%
Universiti Teknologi Malaysia on 2021-02-19 Submitted works	1%
Welyyanti, Des, Edy Tri Baskoro, Rinovia Simanjuntak, and Saladin Uttu Crossref	. 1%
arxiv.org Internet	1%
UIN Syarif Hidayatullah Jakarta on 2022-01-11 Submitted works	1%
Higher Education Commission Pakistan on 2010-01-06 Submitted works	<1%
math.is.tohoku.ac.jp Internet	<1%
coek.info Internet	<1%

rinosimanjuntak.files.wordpress.com Internet	<1
ece.uvic.ca Internet	<1
Higher Education Commission Pakistan on 2015-04-08 Submitted works	<1
Universitas Jember on 2017-02-15 Submitted works	<1
digilib.unila.ac.id Internet	<1
Des Welyyanti, Edy Tri Baskoro, Rinovia Simajuntak, Saladin Uttu ^{Crossref}	nggad <1
Hiroyuki KIMURA. "Free vibration analysis of a string with vibration crossref	on sup <1
media.neliti.com Internet	<1
D Welyyanti, M Azhari, R Lestari. "On Locating Chromatic Numbe Crossref	r of Di <1
María Teresa Signes Pont, Juan Manuel García Chamizo, Higinio Crossref	Mora <1
XUELIAN LI, YUPU HU, JUNTAO GAO. "LOWER BOUNDS ON THE Crossref	SECO <1
"Computer Aided Engineering Design", Springer Science and Bus Crossref	iness <1

21	Higher Education Commission Pakistan on 2018-11-30 Submitted works	<1%
22	Higher Education Commission Pakistan on 2020-02-10 Submitted works	<1%
23	VIT University on 2013-10-09 Submitted works	<1%
24	eprints.gla.ac.uk Internet	<1%