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On X -sub-linearly independent modules

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Abstract. The notion of X -sub-exact sequence of modules is a generalization of exact sequences. Let K, L, M be R -modules and X a submodule of L . The triple (K, L, M) is said to be X -sub-exact at L if $K \rightarrow X \rightarrow M$ is exact at X . The exact sequence is a special case of X -sub-exact by taking $X = L$. We introduce an X -sub-linearly independent module which is a generalization of linearly independent relative to an R -module M by using the concept of X -sub-exact sequence.

1. Introduction

Let R be a ring and let M be an R -module. A subset $S \subseteq M$ is R -linearly dependent if there exist distinct x_1, x_2, \dots, x_n in S and elements a_1, a_2, \dots, a_n of R , not all of which are 0, such that $a_1x_1 + a_2x_2 + \dots + a_nx_n = 0$. A set that is not R -linearly dependent is said to be R -linearly independent [1]. Let N be a left R -module, then N is said linearly independent to R (or N is R -linearly independent) if there exists a monomorphism $\varphi : R^{(\Lambda)} \rightarrow N$ [5].

Suprpto [6] introduced a generalization of linearly independency relative to an R -module M as follows: Let M be an R -module. The family of R -modules $\mathcal{N} = \{N_\lambda\}_\Lambda$ is said to be linearly independent to M if there exist a monomorphism $f : \coprod_\Lambda N_\lambda \rightarrow M$. If $\{N_\lambda = N\}_\Lambda$, then $f : N^{(\Lambda)} \rightarrow M$. We can say that $\mathcal{N} = \{N_\lambda\}_\Lambda$ is linearly independent to M if the sequence $0 \rightarrow \coprod_\Lambda N_\lambda \xrightarrow{f} M$ is exact at $\coprod_\Lambda N_\lambda$.

Let R be a ring and let $A \xrightarrow{f} B \xrightarrow{g} C$ be an exact sequence of R -modules, i.e. $Im f = Ker g (= g^{-1}(\{0\}))$. We can generalize the submodule $\{0\}$ to any submodule $U \subseteq C$ as we refer to [2] in which Davvaz and Parnian-Garamaleky introduced the concept of quasi-exact sequences.

A sequence of R -modules and R -homomorphisms $A \xrightarrow{f} B \xrightarrow{g} C$ is quasi-exact in B or U -exact in B if there exists a submodule U in C such that $Im f = g^{-1}(U)$.

Then, Anvariye dan Davvaz [7] proved further results about quasi-exact sequences and introduced generalization of Schanuel Lemma. Moreover, they obtained some relationships between quasi-exact sequences and superfluous (or essential) submodules.

Furthermore, Davvaz and Shabani-Solt introduced a generalization of some notions in homological algebra [3]. They gave a generalization of the Lambek Lemma, Snake Lemma, connecting homomorphism and exact triangle and they established new basic properties of the U -homological algebra. In [8], Anvariye dan Davvaz studied U -split sequences and established several connections between U -split sequences and projective modules.



Let K, L, M be R -modules and X a submodule of L . The triple (K, L, M) is said to be an X -sub-exact at L if

$$K \rightarrow X \rightarrow M$$

is exact, i.e. $Im f = Ker g$. The exact sequence is a special case of X -sub-exact by taking $X = L$ [4].

In this paper, we introduce an X -sub-linearly independent module which is a generalization of linearly independent relative to an R -module M by using the concept of X -sub-exact sequence.

Let M be an R -module. The family of R -modules $\mathcal{N} = \{N_\lambda\}_\Lambda$ is said to be X -sub-linearly independent to M if the triple $(0, \coprod_\Lambda N_\lambda, M)$ is X -sub-exact (where X is a submodule of $\coprod_\Lambda N_\lambda$). Then, we collect all submodules X of $\coprod_\Lambda N_\lambda$ such that \mathcal{N} is X -sub-linearly independent to M , we denote it by $\sigma(0, \coprod_\Lambda N_\lambda, M)$. In this paper, we give some basic properties of X -sub-linearly independent modules and $\sigma(0, \coprod_\Lambda N_\lambda, M)$. We will show that $\sigma(0, \coprod_\Lambda N_\lambda, M)$ is closed under submodules and intersections. Furthermore, $\sigma(0, \coprod_\Lambda N_\lambda, M)$ always has a maximal element, for every family of R -modules \mathcal{N} and R -module M . In other words, for every family of R -modules $\mathcal{N} = \{N_\lambda\}_\Lambda$ and R -module M , there exist a submodule X maximal such that \mathcal{N} is an X -sub-linearly independent.

2. Main Results

As a generalization of linearly independent relative to an R -module M , we define X -sub-linearly independent by using the concept of X -sub-exact sequence as follows:

Definition 2.1 Let M be an R -module. The family of R -modules $\mathcal{N} = \{N_\lambda\}_\Lambda$ is said to be X -sub-linearly independent to M if the triple $(0, \coprod_\Lambda N_\lambda, M)$ is X -sub-exact (where X is a submodule of $\coprod_\Lambda N_\lambda$), i.e. the sequence

$$0 \rightarrow X \rightarrow M$$

is exact.

Example 2.1 Let $\mathcal{N} = \{\mathbb{Z}_2, \mathbb{Z}_5\}$ the family of \mathbb{Z} -modules and let \mathbb{Z}_6 be \mathbb{Z} -module. We define $f : \mathbb{Z}_2 \rightarrow \mathbb{Z}_6$, where $f(0) = 0$ and $f(1) = 3$. So, f is a monomorphism. Hence, the sequence

$$0 \rightarrow \mathbb{Z}_2 \xrightarrow{f} \mathbb{Z}_6$$

is exact. Therefore, the triple $(0, \mathbb{Z}_2 \oplus \mathbb{Z}_5, \mathbb{Z}_6)$ is \mathbb{Z}_2 -sub-exact. So, \mathcal{N} is \mathbb{Z}_2 -sub-linearly independent to \mathbb{Z}_6 .

Assume f is a monomorphism from $\mathbb{Z}_2 \oplus \mathbb{Z}_5$ to \mathbb{Z}_6 . Then,

$$0 = f(0, 0) = f(5(0, 1)) = 5f(0, 1).$$

We get $f(0, 1) = f(0, 0) = 0$, a contradiction. So, we can not define a monomorphism from $\mathbb{Z}_2 \oplus \mathbb{Z}_5$ to \mathbb{Z}_6 . Hence \mathcal{N} is not linearly independent to \mathbb{Z}_6 .

Example 2.1 shows that if the family of R -modules \mathcal{N} is an X -sub-linearly independent to an R -module M , for some submodule X of $\coprod_\Lambda N_\lambda$, $N_\lambda \in \mathcal{N}$, for all $\lambda \in \Lambda$, then \mathcal{N} is not necessary linearly independent to M .

We already know that any set that containing 0 is linearly dependent since $1 \cdot 0 = 0$. In the following Proposition, we want to show that the family of R -modules \mathcal{N} is 0 -sub-linearly independent to M , for any R -module M .

Proposition 2.1 Let $\mathcal{N} = \{N_\lambda\}_\Lambda$ be a family of R -modules. Then \mathcal{N} is 0-sub-linearly independent to M , for any R -module M .

Proof. Since the sequence $0 \rightarrow 0 \rightarrow M$ is exact, the triple $(0, \coprod_\Lambda N_\lambda, M)$ is 0-sub-exact at $\coprod_\Lambda N_\lambda$. Hence, \mathcal{N} is 0-sub-linearly independent to M . \square

In fact, we can define a monomorphism from R -module M to itself. So, Any R -module M is M -sub-linearly independent relative to M . We already know that any subset of a linearly independent set is linearly independent. In the following proposition, we will prove that M is X -sub-linearly independent to M , for every submodule X of M .

Proposition 2.2 For any R -module M , M is X -sub-linearly independent to M , for every submodule X of M .

Proof. Let M be an R -module and let X be a submodule of M . We have the inclusion $i : X \rightarrow M$ such that the sequence $0 \rightarrow X \xrightarrow{i} M$ is exact. Hence, the triple $(0, M, M)$ is X -sub-exact. Therefore M is X -sub-linearly independent to M . \square

Then, we will give some properties of X -sub-linearly independent relative to an R -module M .

Clearly, we can define a monomorphism from N_λ to $\coprod_\Lambda N_\lambda$. So, we have the following proposition:

Proposition 2.3 Let $\mathcal{N} = \{N_\lambda\}_\Lambda$ be a family of R -modules. Then \mathcal{N} is N_λ -sub-linearly independent to $\coprod_\Lambda N_\lambda$, for every $\lambda \in \Lambda$.

Proof. For every $\lambda \in \Lambda$, we have the inclusion $i : N_\lambda \rightarrow \coprod_\Lambda N_\lambda$ such that the sequence $0 \rightarrow N_\lambda \xrightarrow{i} \coprod_\Lambda N_\lambda$ is exact. Therefore, the triple $(0, \coprod_\Lambda N_\lambda, \coprod_\Lambda N_\lambda)$ is N_λ -sub-exact at $\coprod_\Lambda N_\lambda$. So, \mathcal{N} is N_λ -sub-linearly independent to $\coprod_\Lambda N_\lambda$, for every $\lambda \in \Lambda$. \square

Since for any submodule X of N_λ , we can define a monomorphism from X to $\coprod_\Lambda N_\lambda$, we have the following proposition.

Proposition 2.4 Let $\mathcal{N} = \{N_\lambda\}_\Lambda$ be a family of R -modules. Then, for every $\lambda \in \Lambda$, \mathcal{N} is X -sub-linearly independent to N_λ for any submodule X of N_λ .

Proof. Let X be a submodule of $N_\lambda \subset \coprod_\Lambda N_\lambda$. We have the inclusion $i : X \rightarrow N_\lambda$ such that the sequence $0 \rightarrow X \rightarrow N_\lambda$ is exact. This implies the triple $(0, \coprod_\Lambda N_\lambda, N_\lambda)$ is X -sub-exact sequence at $\coprod_\Lambda N_\lambda$. Hence \mathcal{N} is X -sub-linearly independent to N_λ . \square

Let K, L, M be R -modules. We define

$$\sigma(K, L, M) = \{X \leq L \mid (K, L, M) \text{ } X\text{-sub-exact at } L\}.$$

Then $\sigma(K, L, M) \neq \emptyset$ since $0 \in \sigma(K, L, M)$.

Let \mathcal{N} be a family of R -modules. If we take $K = 0$, $L = \coprod_{\Lambda} N_{\lambda}$ and $K = M$, then

$$\begin{aligned} \sigma(0, \coprod_{\Lambda} N_{\lambda}, M) &= \{X \leq L \mid (0, L, M) \text{ is } X\text{-sub-exact at } L\} \\ &= \{X \leq L \mid \mathcal{N} \text{ is } X\text{-sub-linearly independent to } M\}. \end{aligned}$$

We recall the properties of $\sigma(0, L, M)$ as follows:

Proposition 2.5 [4] *Let L, M be two R -modules and X_{λ} be a submodule of L , for every $\lambda \in \Lambda$. If $X_{\lambda} \in \sigma(0, L, M)$, for every $\lambda \in \Lambda$, then $\cap_{\Lambda} X_{\lambda} \in \sigma(0, L, M)$.*

In the following Proposition, we will prove that $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$ is closed under intersections, i.e. if $X_i \in \sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$, for every $i \in I$, then $\cap_{i \in I} X_i \in \sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$.

Proposition 2.6 *Let $\mathcal{N} = \{N_{\lambda}\}_{\Lambda}$ be a family of R -modules and let M be an R -module. If \mathcal{N} is X_i -sub-linearly independent to M , for every $i \in I$, then \mathcal{N} is $\cap_{i \in I} X_i$ -sub-linearly independent to M . In other words, $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$ is closed under intersections.*

Proof. Since \mathcal{N} is X_i -sub-linearly independent to M , for every $i \in I$, then the triple $(0, \coprod_{\Lambda} N_{\lambda}, M)$ is X_i -sub-exact. Therefore, $X_i \in \sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$, for every $i \in I$. By Proposition 2.5, we get $\cap_{i \in I} X_i \in \sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$. So, \mathcal{N} is $\cap_{i \in I} X_i$ -sub-linearly independent to M . \square

Furthermore, in the following proposition, we want to show that $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$ is closed under submodules.

Proposition 2.7 *Let $\mathcal{N} = \{N_{\lambda}\}_{\Lambda}$ be a family of R -modules and M be an R -module. If \mathcal{N} is X -sub-linearly independent to M , then \mathcal{N} is X' -sub-linearly independent to M , for every submodule X' of X . In other words, $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$ is closed under submodules.*

Proof. Since \mathcal{N} is X -sub-linearly independent to M , then there is a monomorphism $f : X \rightarrow M$. Let X' be a submodule of X . Then, we can define the inclusion $i : X' \rightarrow X$. So, $f \circ i : X' \rightarrow M$ is a monomorphism. Hence, \mathcal{N} is X' -sub-linearly independent to M . Therefore, if $X \in \sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$, then $X' \in \sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$, for every submodule X' of X . \square

We already know that a basis for a free R -module F is a maximal linearly independent set in R -module F . So, we will investigate the maximal element of $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$, i.e the maximal subset X of $\coprod_{\Lambda} N_{\lambda}$ such that \mathcal{N} is X -sub-linearly independent to an R -module M . If there is a monomorphism $f : \coprod_{\Lambda} N_{\lambda} \rightarrow M$, then $\coprod_{\Lambda} N_{\lambda}$ is the maximal element in $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$, i.e. for every $X \in \sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$, if $\coprod_{\Lambda} N_{\lambda} \subseteq X$, then $\coprod_{\Lambda} N_{\lambda} = X$. But, $\coprod_{\Lambda} N_{\lambda}$ is not necessary belong to $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$.

The most important criterion for the existence of maximal elements in a partially ordered set is Zorn's lemma. We recall Zorn's lemma as follows:

Proposition 2.8 (Zorn's Lemma)[1] *Let X be a partially ordered set and assume that every chain in X has an upper bound. Then X has a maximal element.*

By using Zorn's lemma, we want to show that there exist a submodule X in $\coprod_{\Lambda} N_{\lambda}$ maximal such that \mathcal{N} is an X -sublinearly independent to M , for every family of R -modules \mathcal{N} and R -module M .

Theorem 2.1 Let $\mathcal{N} = \{N_{\lambda}\}_{\Lambda}$ be a family of R -modules and M be an R -module. Then there exist a submodule X in $\coprod_{\Lambda} N_{\lambda}$ maximal such that \mathcal{N} is an X -sublinearly independent to M . In other words, $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$ always has a maximal element.

Proof. Let $\mathcal{X} = \{X | X \subseteq \coprod_{\Lambda} N_{\lambda} \text{ and } X \subseteq M\}$. The set \mathcal{X} is not empty since $0 \in \mathcal{X}$. Let $\{X_i\}_{i \in I}$ be a chain (totally ordered set) in \mathcal{X} . Let $Y = \bigcup_{i \in I} X_i$, where $X_i \in \mathcal{X}$, for all $i \in I$. As a set, Y certainly contains all the X_i 's. Since a union of submodules is not usually a submodule, we will show that Y is a submodule of $\coprod_{\Lambda} N_{\lambda}$.

If x and y are in Y , then $x \in X_i$ and $y \in X_j$, for two of the submodules X_i and X_j of $\coprod_{\Lambda} N_{\lambda}$. Since the set of submodules $\{X_i\}_{i \in I}$ is totally ordered,

$$X_i \subset X_j \text{ or } X_j \subset X_i.$$

Without loss of generality, $X_i \subset X_j$. Therefore x and y are in X_j , so $x + y \in X_j \subset Y$ and $rx \in X_j \subset Y$, for every $r \in R$. We can conclude that $Y = \bigcup_{i \in I} X_i$ is a submodule of $\coprod_{\Lambda} N_{\lambda}$. Similarly, we obtain Y is a submodule of M .

Since Y contains every X_i , for all $i \in I$, Y is an upper bound on the totally ordered set $\{X_i\}_{i \in I}$. By Zorn's lemma, \mathcal{X} contains a maximal element. This maximal element is a submodule of $\coprod_{\Lambda} N_{\lambda}$ and M that is maximal for inclusion among all submodule of $\coprod_{\Lambda} N_{\lambda}$ and M . We can conclude that there exist a submodule X in $\coprod_{\Lambda} N_{\lambda}$ maximal such that \mathcal{N} is an X -sublinearly independent to M or $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$ always has a maximal element. \square

3. Conclusion

The family of R -modules $\mathcal{N} = \{N_{\lambda}\}_{\Lambda}$ is an X -sub-linearly independent to M if the triple $(0, \coprod_{\Lambda} N_{\lambda}, M)$ is X -sub-exact (where X is a submodule of $\coprod_{\Lambda} N_{\lambda}$). If we take $X = \coprod_{\Lambda} N_{\lambda}$, then $\mathcal{N} = \{N_{\lambda}\}_{\Lambda}$ is linearly independent. Hence, sub-linearly independent module is a generalization of linearly independent module.

Then, we collect all submodules X of $\coprod_{\Lambda} N_{\lambda}$ such that \mathcal{N} is X -sub-linearly independent to M , we denote it by $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$. We have proved that $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$ is closed under submodules and intersections. Furthermore, for every family of R -modules $\mathcal{N} = \{N_{\lambda}\}_{\Lambda}$ and R -module M , there exist X maximal such that \mathcal{N} is an X -sublinearly independent. In other words, $\sigma(0, \coprod_{\Lambda} N_{\lambda}, M)$ always has a maximal element, for every family of R -modules \mathcal{N} and R -module M .

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