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To cite this article: D Putri et al 2021 J. Phys.: Conf. Ser. 1751 012024

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# Determining the Number of Disconnected Vertices Labeled Graphs of Order Six with the Maximum Number Twenty **Parallel Edges and Containing No Loops**

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1751 (2021) 012024

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Abstract. If there exist two vertices on a given graph that are not connected by a path, then we call that graph is disconnected. Given a graph with n vertices and m edges, then a lot of graphs can be constructed. In this paper, we discuss the number of disconnected vertices labeled graphs of order six (n = 6) with the maximum number of parallel edges is twenty. Moreover, a maximum 3 umber of edges that connect different pair of vertices is ten (parallel edges are counted as one) and ontaining no loops (isomorphic graphs are counted as one).

Keyword: counting graph, disconnected graph, vertices labelled graph.

#### 1. Introduction

Historically, graph enumeration had been done by Cayley in 1874 [1]. Cayley used the concept of tree in his way to enumerating the number of the isomer of hydrocarbon C<sub>n</sub>H<sub>2n +2</sub> [2]. The basic concept of labeling and the enumerating graph was given by Harary and Palmer [3]. There are many ways to construct the disconnected graph of order n, m edges, and t edges that connecting the different pairs of vertices. In 2016, the number of disconnected vertices labeled graphs containing no parallel edges is observed [4], and in 2017, the number of disconnected vertices labeled graph of order maximum four is discussed [5]. Wamilana et al. continued their research to determine the number of connected vertices labeled graph of order five with the maximum number of parallel edges is five and containing no loops [6].

. In this paper, we give the general form of the number of disconnected vertices labeled graphs of order six (n = 6), m edges, and t edges that connecting different pairs of vertices, with  $1 \le m \le 20, 1 \le t \le 10$ , and containing no loops (isomorphic graphs are counted as one).

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#### 2. Construction and Observation

Given a graph G of order six (n = 6) with m edges,  $1 \le n \le 20$ , and the number of edges that connect the different vertices or points is t (the number of parallel edges that connect the same pair of points is counted as one), with  $1 \le t \le 10$ . Some of the patterns of a disconnected graph of order 6, m edges and t edges are given in the following table:

**Table 1.** The number of disconnected graph with n = 6, with  $1 \le m \le 20$ ,  $1 \le t \le 10$ .



• the following table shows the number of disconnected graph or order six (n = 6), *m* edges, and *t* edges that connecting the different pair of vertices, with  $1 \le t \le 5$ .

	The numbers of disconnected graphs					
m	<i>t</i> = 1	<i>t</i> = 2	<i>t</i> = 3	<i>t</i> = 4	<i>t</i> = 5	
1	15	-	-	-	-	
2	15	105	-	-	-	
3	15	210	365	-	-	
4	15	315	1095	975	-	
5	15	420	2190	3900	957	
6	15	525	3650	9750	4785	
7	15	630	5475	19500	14355	
8	15	735	7665	34125	33495	
9	15	840	10220	54600	66990	
10	15	945	12140	81900	120582	
11	15	1050	16425	117000	200970	
12	15	1155	20075	160875	315810	
13	15	1260	24090	214500	473715	
14	15	1365	28470	278850	315810	
15	15	1470	33215	354900	957957	
16	15	1575	38325	443625	1306305	
17	15	1680	43800	546000	1741740	
18	15	1785	49640	663000	2277660	

**Table 2.** The number of disconnected graph with n = 6, with  $1 \le m \le 20$ ,  $1 \le t \le 5$ 

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	19	15	1890	55845	795	600	2928420	
	20	15	1995	62415	944	775	3709332	

<sup>6</sup> he following table shows the number of disconnected graph or order six (n = 6), *m* edges, and *t* edges that connecting the different pair of vertices, with  $6 \le t \le 10$ .

**Table 3.** The number of disconnected graph with  $n = 6, 6 \le m \le 20, 6 \le t \le 10$ 

	The numbers of disconnected graphs					
т	<i>t</i> = 6	<i>t</i> = 7	<i>t</i> = 8	<i>t</i> = 9	<i>t</i> = 10	
6	715	-	-	-	-	
7	4290	345	-	-	-	
8	15015	2415	210	-	-	
9	40040	9660	1680	60	-	
10	90090	28980	7560	540	6	
11	180180	72450	25200	2700	60	
12	330330	159390	69300	9900	330	
13	566280	318780	166320	29700	1320	
14	920205	592020	360360	77220	4290	
15	1431430	1036035	720720	180180	12012	
16	2147145	1351350	1351350	386100	30030	
17	3123120	2402400	2402400	772200	68640	
18	4424420	4084080	4084080	1458600	145860	
19	6126120	6683040	6683040	2625480	291720	
20	8314020	10581480	10581480	4534920	554268	

The rember of disconnected graph with n = 6, with  $1 \le m \le 20$ ,  $1 \le t \le 5$  in Table 2 can be represented as follow:

	The numbers of disconnected graphs					
m	<i>t</i> = 1	<i>t</i> = 2	<i>t</i> = 3	<i>t</i> = 4	<i>t</i> = 5	
1	1 × 15	-	-	-	-	
2	$1 \times 15$	$1 \times 105$	-	-	-	
3	$1 \times 15$	$2 \times 105$	$1 \times 365$	-	-	
4	$1 \times 15$	$3 \times 105$	$3 \times 365$	$1 \times 975$	-	
5	$1 \times 15$	$4 \times 105$	$6 \times 365$	$4 \times 975$	$1 \times 957$	
6	$1 \times 15$	$5 \times 105$	$10 \times 365$	$10 \times 975$	$5 \times 957$	
7	$1 \times 15$	$6 \times 105$	15 × 365	$20 \times 975$	$15 \times 957$	
8	$1 \times 15$	$7 \times 105$	21 × 365	$35 \times 975$	$35 \times 957$	
9	$1 \times 15$	$8 \times 105$	$28 \times 365$	$56 \times 975$	$70 \times 957$	
10	$1 \times 15$	9 × 105	$36 \times 365$	$84 \times 975$	$126 \times 957$	
11	$1 \times 15$	$10 \times 105$	45 × 365	$120 \times 975$	$210 \times 957$	
12	$1 \times 15$	$11 \times 105$	55 × 365	165 × 975	$330 \times 957$	
13	$1 \times 15$	$12 \times 105$	66 × 365	$220 \times 975$	$495 \times 957$	
14	$1 \times 15$	$13 \times 105$	$78 \times 365$	$286 \times 975$	$715 \times 957$	
15	$1 \times 15$	$14 \times 105$	91 × 365	$364 \times 975$	$1001 \times 957$	
16	$1 \times 15$	$15 \times 105$	$105 \times 365$	455 × 975	1365 × 957	
17	$1 \times 15$	$16 \times 105$	$120 \times 365$	$560 \times 975$	$1820 \times 957$	
18	$1 \times 15$	$17 \times 105$	136 × 365	$680 \times 975$	$2380 \times 957$	
19	$1 \times 15$	$18 \times 105$	$153 \times 365$	$816 \times 975$	$3060 \times 957$	
20	$1 \times 15$	$19 \times 105$	$171 \times 365$	$969 \times 975$	$3876 \times 957$	

**Table 4.** The number of disconnected graph with n = 6, with  $1 \le m \le 20, 1 \le t \le 5$ 

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The number of disconnected graph with n = 6, with  $1 \le m \le 20, 6 \le t \le 10$  in Table 3 can be represented as follow:

**Table 5.** The number of disconnected graph with  $n = 6, 6 \le m \le 20, 6 \le t \le 10$ 

	The numbers of disconnected graphs						
т	t = 6	<i>t</i> = 7	<i>t</i> = 8	<i>t</i> = 9	<i>t</i> = 10		
6	$1 \times 715$	-	-	-	-		
7	$6 \times 715$	$1 \times 345$	-	-	-		
8	$21 \times 715$	$7 \times 345$	$1 \times 210$	-	-		
9	56 × 715	$28 \times 345$	$8 \times 210$	$1 \times 60$	-		
10	$126 \times 715$	$84 \times 345$	$36 \times 210$	$9 \times 60$	$1 \times 6$		
11	252 × 715	$210 \times 345$	$120 \times 210$	$45 \times 60$	$10 \times 6$		
12	462 × 715	$462 \times 345$	$350 \times 210$	$165 \times 60$	55 × 6		
13	792 × 715	924 × 345	$792 \times 210$	$495 \times 60$	220 × 6		
14	$1287 \times 715$	$1716 \times 345$	$1716 \times 210$	$1287 \times 60$	315 × 6		
15	$2002 \times 715$	$3003 \times 345$	$3432 \times 210$	$3003 \times 60$	$2002 \times 6$		
16	$3003 \times 715$	$5005 \times 345$	$6435 \times 210$	$6435 \times 60$	$5005 \times 6$		
17	4368 × 715	$8008 \times 345$	$11440 \times 210$	$12870 \times 60$	$11440 \times 6$		
18	6188 × 715	$12376 \times 345$	$19440 \times 210$	$24310 \times 60$	24310 × 6		
19	8568 × 715	$18564 \times 345$	$31824 \times 210$	$43758 \times 60$	$48620 \times 6$		
20	$11628 \times 715$	27132 × 345	50388 × 210	$75582 \times 60$	92378 × 6		

#### 3. Result and Discussion

Given a graph G with the number of vertex V is n = 1 the number of edges is m, with  $1 \le m \le 20$ , and the number of edges that connect the different vertices is t (the number of parallel edges that connect the same pair of vertices is counted as one), with  $1 \le t \le 10$ .

After the construction and observation, we get the following results. The disconnected vertices labelled graph with order n, m edges, and t edges that connect the different pairs of vertices is denoted by  $G'(p)_{n,m,t}$ . The number of  $G'(p)_{n,m,t}$  is denoted by  $N(G'(p)_{n,m,t})$ .

**Result 1**. If n = 6, m = 1, 2, ..., 20, and t = 1, then  $N(G'(p)_{6,m,1}) = 15$ .

*Proof.* Based on Tabel 4 column t = 1, we have the following sequence of number:

The sequence form polynomial of order zero, with general form  $a_m = a_0$ . For m = 1, we have  $a_m = 15$ . Therefore, the number of disconnected vertices labelled graph with n = 6, m = 1, 2, ..., 20, and t = 1 is  $N(G'(p)_{6,m,1}) = 15$ .

**Result 2.** If n = 6, m = 2, 3, ..., 20, and t = 2, then  $N(G'(p)_{6,m,2}) = 105 \times C_1^{(m-1)}$ .

*Proof.* Based on Tabel 4 column t = 2, we have the following sequence of number:

Since the fix difference in the sequence occurs in the first order, the general form of the polynomial is

$$a_m = a_1 m + a_0.$$
 (1)  
By substituting  $m = 2$  and 3 to Equation (1), we have:

$$105 = 2a_1 + a_0 \tag{2}$$

$$210 = 3a_1 + a_0 \tag{3}$$

Solving this linearly equation system, we get  $a_0 = -105$ ,  $a_1 = 105$  and hence  $N(G'(p)_{6,m,2}) = 105 \ m - 105 = 105(m-1) = 105 \times C_1^{(m-1)}$ .

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Since the fix difference in the sequence occurs in the second order, the general form of the polynomial is  $a_m = a_2 m^2 + a_1 m + a_0.$ (4)

By substituting 
$$m = 3, 4$$
 and 5 to Equation (4), we have:

$$365 = 9a_2 + 3a_1 + a_0 \tag{5}$$

$$1095 = 16a_2 + 4a_3 + a_3 \tag{6}$$

$$1095 = 16a_2 + 4a_1 + a_0 \tag{6}$$
  
$$2190 = 25a_2 + 5a_1 + a_0 \tag{7}$$

Solving this linearly equation system, we get  $a_2 = \frac{365}{2}$ ,  $a_1 = -\frac{1095}{2}$ ,  $a_0 = \frac{730}{2}$  and hence  $N(G'(p)_{6,m,3}) = \frac{365}{2}m^2 - \frac{1095}{2}m + \frac{730}{2} = 365 \times C_2^{(m-1)}$ .

**Result 4**. For n = 6, m = 4, 5, ..., 20, and t = 4,  $N(G'(p)_{6,m,4}) = 975 \times C_3^{(m-1)}$ . *Proof.* 

Based on Table 4 column t = 4 and m = 4, 5, ..., 20, we get the following sequence: 1, 4, 10, 20, 35, 56, 84, 120, 165, 220, 286, 364, 455, 560, 680, 816, 969. This sequence is related to arithmetic polynomial of order three.

1 4 10 20 35 56 84 120 165	 560 680 816 969
3 6 10 15 21 28 36 45	 120 136 153
3 4 5 6 7 8 9	 16 17
1 1 1 1 1 1	 1

Since the fix difference in the sequence occurs in the third order, the general form of the polynomial is  $a_m = a_3 m^3 + a_2 m^2 + a_1 m + a_0.$ (8)

By substituting m = 4, 5, 6 and 7 to Equation (8), we have:

$$975 = 64a_3 + 16a_2 + 4a_1 + a_0 \tag{9}$$
  
$$3900 = 125a_3 + 25a_2 + 5a_1 + a_0 \tag{10}$$

$$9750 = 216a_3 + 36a_2 + 6a_1 + a_0 \tag{11}$$

$$10500 = 242a_1 + 40a_2 + 7a_1 + a_0 \tag{12}$$

 $19500 = 343a_3 + 49a_2 + 7a_1 + a_0$ (12) Solving this linearly equation system, we get  $a_3 = \frac{19500}{12}$ ,  $a_2 = -\frac{11700}{12}$ ,  $a_1 = \frac{21450}{12}$ ,  $a_0 = -\frac{11700}{12}$  and hence

 $N(G'(p)_{6,m,4}) = \frac{19500}{12}m^3 - \frac{11700}{12}m^2 + \frac{21450}{12}m - \frac{11700}{12} = 975 \times C_3^{(m-1)}.$ In a similar way as the Result 1-4, we can provide the following formulas: **Result 5.** For n = 6, m = 5, 6, ..., 20, and  $t = 5, N(G'(p)_{6,m,5}) = 957 \times C_4^{(m-1)}.$ **Result 6.** For n = 6, m = 6, 7, ..., 20, and  $t = 6, N(G'(p)_{6,m,6}) = 715 \times C_5^{(m-1)}.$ **Result 7.** For n = 6, m = 7, 8, ..., 20, and  $t = 7, N(G'(p)_{6,m,7}) = 345 \times C_6^{(m-1)}.$ **Result 8.** For n = 6, m = 8, 9, ..., 20, and  $t = 8, N(G'(p)_{6,m,8}) = 210 \times C_7^{(m-1)}.$ **Result 9.** For n = 6, m = 9, 10, ..., 20, and  $t = 9, N(G'(p)_{6,m,9}) = 60 \times C_8^{(m-1)}.$ **Result 10.** For n = 6, m = 10, 11, ..., 20, and  $t = 10, N(G'(p)_{6,m,10}) = 6 \times C_9^{(m-1)}.$ 

#### 4. Conclussion

From the results, we can conclude that the number of disconnected vertices labeled graphs of order six (n = 6), m edges and t edges that connecting different pairs of vertices, with  $1 \le m \le 20$ ,  $1 \le t \le 10$ ,  $t \le m$ , and

containing no loops is  $N(G'(p)_{6,m,t}) = k_t \times C_{(t-1)}^{(m-1)}$ , where  $k_1 = 15$ ,  $k_2 = 105$ ,  $k_3 = 365$ ,  $k_4 = 975$ ,  $k_5 = 957$ ,  $k_6 = 715$ ,  $k_7 = 345$ ,  $k_8 = 210$ ,  $k_9 = 60$ , and  $k_{10} = 6$ .

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