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# Determining the Noetherian Property of Generalized Power Series Modules by Using $X$ -Sub-Exact Sequence

A Faisal<sup>1</sup>, Fitriani<sup>2</sup>, and Sifriyani<sup>3</sup>

<sup>1,2</sup>Department of Mathematics, Universitas Lampung, Bandar Lampung, Indonesia

<sup>3</sup>Department of Mathematics, Universitas Mulawarman, Samarinda, Indonesia

**email:** ahmadfaisal@fmipa.unila.ac.id<sup>1</sup>, fitriani.1984@fmipa.unila.ac.id<sup>2</sup>, sifriyani@fmipa.unmul.ac.id<sup>3</sup>

**Abstract.** The Noetherian property of the generalized power series module can determine in several ways. This paper uses the sub-exact sequence of modules over a ring  $R$  to determine this property. This investigation not only determines the Noetherian property of the generalized power series module but also the Noetherian property of its submodule. Furthermore, we give a construction of  $R[[S]]$ -homomorphism between the generalized power series modules.

**Keyword:** noetherian, strictly ordered monoid, generalized power series modules, exact sequence, sub-exact sequence.

## 1. Introduction

The exact sequence of modules is one of the essential concepts in module theory [1], [2]. In [3], Fitriani et al. introduced a sub-exact sequence of modules. This concept is motivated by the quasi exact sequence established by Davvaz and Parnian-Garamaleky [4]. Furthermore, they use this concept to generalize the generator of modules related to a family of modules over a ring  $R$  [5]. Moreover, using a generalization of a linearly independent set of modules [6], they obtained a basis and free modules related to a family of modules [7].

Given ring  $R$ , monoid  $(S, \leq)$  with a strictly ordered, and a monoid homomorphism  $\omega$  from  $S$  to  $\text{End}(R)$ . In 2019, Faisal and Fitriani gave some conditions for skew GPSM to be a  $T[[S, \omega]]$ -Noetherian module over a ring  $R[[S, \omega]]$  [8]. This sufficient condition is a generalization of the previous results [9], which were obtained by applying the properties in [10], generalizing the sufficient conditions in [11], and using the relations specified in [12].

Varadarajan [13] introduce the generalized power series module (GPSM). This module is a module over the generalized power series ring (we call it by GPSR), introduced by Ribenboim [14]. Moreover, the results of Ribenboim construction were generalized by Mazurek and Ziembowski [15] by utilizing the monoid homomorphism used in the convolution multiplication operation. In addition to constructing GPSM, Varadarajan [16] also provides necessary and sufficient conditions that GPSM is a Noetherian module. In this paper, we give a method to determine the Noetherian property of the generalized power series module. We use the concept of the sub-exact sequence to determine this property. In this way, we also can determine the Noetherian property of its submodules. Moreover, we give a construction of  $R[[S]]$ -homomorphism between the generalized power series modules.



**2. The Main Results**

Let  $R$  be a commutative ring with  $1_R \in R$  and  $S$  be a monoid with strictly ordered. Let  $N_1, N_2,$  and  $N_3$  be three modules over ring  $R$ . The set  $N_i[[S]]$  consists of all function  $\mu$  from  $S$  to  $N_i$  such that the support of  $f$  is Artinian and narrow (we denote support of  $f$  by  $\text{supp}(f)$ , that is the set of  $s \in S$ , where  $f(s)$  is not equal to 0), for  $i = 1, 2, 3$ . We can write the set as follow:

$$N_i[[S]] = \{\mu : S \rightarrow N_i \mid \text{supp}(\mu) \text{ is Artinian and narrow}\},$$

$i = 1, 2, 3$ .

Before we give a condition when a submodule  $L[[S]]$  of  $N_2[[S]]$  is Noetherian  $R[[S]]$ -module, we recall that if  $L$  is a submodule of  $N$ , then  $L[[S]]$  is a submodule of  $N_2[[S]]$  as a module over  $R[[S]]$ . Let

$$L[[S]] = \{\mu \in N_2[[S]] \mid \mu(s) \in L, \text{ for all } s \in S\}.$$

The set  $L[[S]]$  is a submodule of  $N_2[[S]]$ .

Let  $K, L, M$  be  $R$ -modules and  $X$  be  $R$ -submodules of  $L$ . Recall that the triple  $(K, L, M)$  is said to be  $X$ -sub-exact at  $L$  if there exist  $f$  and  $g$  such that the sequence  $K \xrightarrow{f} X \xrightarrow{g} M$  is exact. In the following proposition, we give a condition when a submodule  $L[[S]]$  of  $N_2[[S]]$  is Noetherian.

**Proposition 1.** Let  $R$  be a commutative ring with  $1 \in R$  and  $(S, \leq)$  be a monoid with a strictly ordered. Let  $N_1, N_2,$  and  $N_3$  are  $R$ -modules, and  $L$  is a submodule of  $N_2$  over  $R$ . If the triple  $(N_1[[S]], N_2[[S]], N_3[[S]])$  is  $L[[S]]$ -sub-exact as an  $R[[S]]$ -module,  $N_1[[S]]$  and  $N_3[[S]]$  are Noetherian  $R[[S]]$ -modules, then  $L[[S]]$  is a Noetherian  $R[[S]]$ -module.

**Proof.** Since the triple  $(N_1[[S]], N_2[[S]], N_3[[S]])$  is  $L[[S]]$ -sub-exact, based on [3], we have the following sequence of a module over  $R[[S]]$  is exact.

$$N_1[[S]] \rightarrow L[[S]] \rightarrow N_3[[S]] \tag{1}$$

Since (1) is exact, there are  $R[[S]]$ -homomorphism  $f$  and  $g$ , where  $f$  is an  $R[[S]]$ -homomorphism from  $N_1[[S]]$  to  $L[[S]]$ ,  $g$  is an  $R[[S]]$ -homomorphism from  $L[[S]]$  to  $N_3[[S]]$ , and  $\text{Im}(f) = \text{Ker}(g)$ . By hypothesis,  $N_1[[S]]$  and  $N_3[[S]]$  are Noetherian modules over  $R[[S]]$ . Hence based on [17], we have  $N[[S]]$  is a Noetherian as a module over  $R[[S]]$ .

Given three  $R$ -modules  $N_1, N_2,$  and  $N_3$ . Fitriani et al. [3] construct a set  $\sigma(N_1, N_2, N_3)$  that consists of all submodules  $X$  of  $N_2$  such that the triple  $(N_1, N_2, N_3)$  is an  $X$ -sub-exact at  $N_2$ , i.e.:

$$\sigma(N_1, N_2, N_3) = \{X \text{ submodule of } N_2 \mid (N_1, N_2, N_3) \text{ is an } X\text{-sub exact at } N_2\}.$$

In this case, we construct the set  $\sigma(N_1[[S]], N_2[[S]], N_3[[S]])$  that consist of all submodules  $X$  of  $N_2[[S]]$  such that the triple of generalized power series modules  $(N_1[[S]], N_2[[S]], N_3[[S]])$  is an  $X$ -sub exact at  $N_2[[S]]$ , i.e.:  $\sigma(N_1[[S]], N_2[[S]], N_3[[S]]) = \{X \leq N_2[[S]] \mid \text{the triple } (N_1[[S]], N_2[[S]], N_3[[S]]) \text{ is an } X\text{-sub exact at } N_2[[S]]\}$ .

As a direct consequence of Proposition 1, we have the following result.

**Corollary 1.** Let  $R$  be a commutative ring with  $1 \in R$  and  $(S, \leq)$  be a monoid with strictly ordered. Let  $M_1, M_2,$  and  $M_3$  are modules over ring  $R$ . If  $N_1[[S]]$  and  $N_3[[S]]$  are Noetherian modules over  $R[[S]]$ , then a submodule  $X$  of  $N_2$  is Noetherian, for every  $X \in \sigma(N_1[[S]], N_2[[S]], N_3[[S]])$ .

**Proof.** Let  $X \in \sigma(N_1[[S]], N_2[[S]], N_3[[S]])$ . We have the following exact sequence of  $R[[S]]$ -modules:

$$N_1[[S]] \rightarrow X \rightarrow N_3[[S]]$$

From Proposition 1, we have  $X$  is Noether.

In [18], Ziemkowski gives a construction of a homomorphism of skew GPSR. Based on his construction, we construct a homomorphism of generalized power series modules in the following proposition.

**Proposition 2.** Given a commutative ring  $R$  with identity element 1. Given a monoid  $(S, \leq)$  with a strictly ordered, an endomorphism  $\omega$  of  $S$  such that for every subset Artinian and narrow  $T \subseteq S$ ,  $\omega(T)$

is Artinian, narrow, and  $h(\omega^{-1}(x)) = h(x)$ , for every  $x$  is in  $S$ , and  $h$  is in  $R[[S]]$ . Let  $\varphi$  be an  $R$ -homomorphism from  $N_2$  to  $N_3$ , where  $N_2, N_3$  be  $R$ -modules. For  $\mu \in N_2[[S]]$ , we define:

$$\begin{aligned} \phi: N_2[[S]] &\rightarrow N_3[[S]] \\ \mu &\mapsto \bar{\mu}, \end{aligned}$$

where

$$\bar{\mu}(x) = \begin{cases} \varphi \circ \mu \circ \omega^{-1}(x) & ; \text{ if } x \in \omega(S), \\ 0 & ; \text{ otherwise.} \end{cases} \dots\dots\dots (1)$$

Then  $\phi$  is an  $R[[S]]$ -homomorphism from  $N_2[[S]]$  to  $N_3[[S]]$ .

**Proof.** Since  $\text{supp}(\bar{\mu}) \subseteq \omega(\text{supp}(\mu))$ , we have  $\bar{\mu} \in N_3[[S]]$ . Now, we will show that  $\phi$  is a  $R[[S]]$ -homomorphism from  $N_2[[S]]$  to  $N_3[[S]]$ .

a. Let  $\mu, \beta \in N_2[[S]]$ , and  $x \in S$ . By (1), we have:

$$\begin{aligned} \overline{\mu + \beta}(x) &= \varphi \circ (\mu + \beta) \circ \omega^{-1}(x) \\ &= \varphi((\mu + \beta) \circ \omega^{-1}(x)) \\ &= \varphi(\mu(\omega^{-1}(x)) + \beta(\omega^{-1}(x))) \\ &= \varphi(\mu(\omega^{-1}(x))) + \varphi(\beta(\omega^{-1}(x))) \\ &= \varphi \circ \mu \circ \omega^{-1}(x) + \varphi \circ \beta \circ \omega^{-1}(x) \\ &= \bar{\mu}(x) + \bar{\beta}(x). \end{aligned}$$

This equation implies that  $\overline{\mu + \beta} = \bar{\mu} + \bar{\beta}$ , and hence  $\phi(\mu + \beta) = \phi(\mu) + \phi(\beta)$ , for every  $\mu, \beta \in N_2[[S]]$ .

b. Let  $\mu \in N_2[[S]]$ ,  $h \in R[[S]]$ , and  $x \in S$ . By (1), we get:

$$\begin{aligned} \overline{h\mu}(x) &= \varphi \circ (h\mu) \circ \omega^{-1}(x) \\ &= \varphi((h\mu)(\omega^{-1}(x))) \\ &= \varphi(\sum_{s+t=\omega^{-1}(x)} h(s) \mu(t)) \\ &= \sum_{s+t=\omega^{-1}(x)} \varphi(h(s)\mu(t)) \\ &= \sum_{s+t=\omega^{-1}(x)} h(s) \varphi(\mu(t)) \\ &= \sum_{\omega^{-1}(u)+\omega^{-1}(v)=\omega^{-1}(x)} h(\omega^{-1}(u)) \varphi(\mu(\omega^{-1}(v))) ; s = \omega^{-1}(u) \text{ dan } t = \omega^{-1}(v) \\ &= \sum_{\omega^{-1}(u)+\omega^{-1}(v)=\omega^{-1}(x)} h(u) \varphi(\mu(\omega^{-1}(v))) ; h(\omega^{-1}(u)) = h(u) \\ &\quad \omega^{-1}(u+v)=\omega^{-1}(x) \\ &\quad u+v=x \\ &= \sum_{u+v=x} h(u) (\varphi \circ \mu \circ \omega^{-1})(v) \\ &= \sum_{u+v=x} h(u) \bar{\mu}(v) \\ &= h\bar{\mu}(x). \end{aligned}$$

Hence, for every  $\mu \in N_2[[S]]$ ,  $h \in R[[S]]$ , we have  $\phi(h\mu) = \overline{h\mu} = h\bar{\mu} = h \phi(\mu)$ .

From a-b, we can conclude that  $\phi$  is an  $R[[S]]$ -homomorphism from  $N_2[[S]]$  to  $N_3[[S]]$ .

Given an  $R$ -module  $M$ , we recall that a submodule  $N$  of  $M$  is a direct summand of  $M$  if there exists  $K \leq M$  such that  $M = N \oplus K$ , i.e.,  $M = N + K$ , and  $N \cap K = 0$ . In this case, every  $m \in M$  can be uniquely written as  $m = a + b$ , where  $a \in N$ , and  $b \in K$  [17]. Next, we will use the construction of  $R[[S]]$ -homomorphism in Proposition 2 to provide the Noetherian property of the GPSM.

**Proposition 3.** Given a commutative ring  $R$  with  $1 \in R$  and a monoid  $(S, \leq)$  with a strictly ordered. Let  $N_1, N_2$ , and  $N_3$  are  $R$ -modules, and  $L[[S]]$  is a direct summand of  $N_2[[S]]$  as an  $R[[S]]$ -module. If  $(N_1[[S]], N_2[[S]], N_3[[S]])$  is  $L[[S]]$ -sub-exact as an  $R[[S]]$ -module,  $N_1[[S]]$  and  $N_3[[S]]$  are Noetherian  $R[[S]]$ -modules, then  $N_2[[S]]$  is Noether.

**Proof.** By hypothesis  $(N_1[[S]], N_2[[S]], N_3[[S]])$  is  $L[[S]]$ -sub-exact as an  $R[[S]]$ -module. Since  $N_1[[S]]$  and  $N_3[[S]]$  are Noetherian  $R[[S]]$ -modules, based on Proposition 1, we get  $L[[S]]$  is Noether. Since  $L[[S]]$  is a direct summand, there exists a submodule  $K$  of  $N_2[[S]]$  such that  $N_2[[S]] = L[[S]] \oplus K$ . Then every  $\mu \in N_2[[S]]$  can uniquely write as  $\mu = \mu' + \mu''$ , where  $\mu' \in L[[S]]$  and  $\mu'' \in K$ . Besides that, the triple  $(N_1[[S]], N_2[[S]], N_3[[S]])$  is  $L[[S]]$ -sub-exact implies that there are two  $R[[S]]$ -homomorphisms  $f$  and  $g$  such that the following sequence is exact.

$$N_1[[S]] \xrightarrow{f} L[[S]] \xrightarrow{g} N_3[[S]],$$

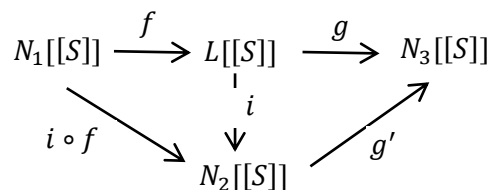
i.e.,  $\text{Im}(f) = \text{Ker}(g)$ .

Thus, we can define an  $R[[S]]$ -homomorphism

$$g': N_2[[S]] \rightarrow N_3[[S]],$$

where  $g' = \begin{cases} g(\mu); & \text{if } \mu \in L[[S]]; \\ 0 & ; \text{ otherwise.} \end{cases}$

Hence, we get the following diagram of  $R[[S]]$ -module:



Based on [3], the following sequence of  $R[[S]]$ -module is exact.

$$N_1[[S]] \xrightarrow{i \circ f} N_2[[S]] \xrightarrow{g'} N_3[[S]].$$

Since  $N_1[[S]]$  and  $N_3[[S]]$  are Noetherian, based on Proposition 1,  $N_2[[S]]$  is Noetherian.

### Conclusion

Based on the results, we can conclude that we can use the concept of a sub-exact sequence of modules over  $R[[S]]$  to determine the Noetherian property of generalized power series modules. Besides that, we also can determine the Noetherian property of its submodule.

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