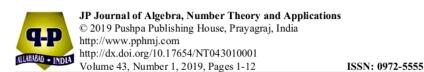
# 2019 (Thompson)--JPANTA--T[[S]]-Noetherian Property on GPSM

By Ahmad Faisol



### T[[S]]-NOETHERIAN PROPERTY ON GENERALIZED POWER SERIES MODULES

#### Ahmad Faisol<sup>1,2</sup>, Budi Surodjo<sup>1</sup> and Sri Wahyuni<sup>1</sup>

<sup>1</sup>Department of Mathematics Universitas Gadjah Mada Sekip Utara BLS 21, Sleman Yogyakarta, Indonesia

<sup>2</sup>Department of Mathematics Universitas Lampung Jl. Prof. Soemantri Brojonegoro No. 1 Bandar Lampung, Lampung, Indonesia

#### Abstract

In this paper, we study the sufficient conditions on a ring R, a multiplicative set  $T \subseteq R$ , strictly ordered monoid  $(S, \leq)$  and an R-module M such that the generalized power series module M[[S]] is a T[[S]]-Noetherian R[[S]]-module, where T[[S]] is a multiplicative subset of generalized power series ring R[[S]].

#### 1. Introduction

Anderson and Dumitrescu [2] introduced the definition of T-Noetherian rings and modules. For any multiplicatively closed subset T of a ring R, a

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ring R is called T-Noetherian if each ideal of R is T-finite, i.e., if  $T \subseteq J \subseteq I$  for some finitely generated ideal J of R and some  $t \in T$ . An R-module M is called an T-Noetherian module if for each submodule N of M, there exist an element  $t \in T$  and a finitely generated submodule N of M such that  $Nt \subseteq F \subseteq N$ . Some properties of N-Noetherian modules are studied by Baeck et al. [3]. Varadarajan [4] constructs the generalized power series modules (GPSM) M[S], which is a module over generalized power series rings (GPSR) N[S] constructed by Ribenboim [6]. Moreover, Varadarajan determined the necessary and sufficient conditions for GPSM N[S] to be a Noetherian module, which strengthens earlier results of Ribenboim.

In this paper, we investigate the sufficient conditions for R[[S]]-module M[[S]] to be T[[S]]-Noetherian.

#### 2. GPSR and GPSM

In this section, we recall the construction of GPSR and GPSM as follows from Ribenboim [6] and Varadarajan [4].

Regarding ordered sets, strictly ordered monoids, Artinian and narrow sets, we will be following the terminology in [6] and [7].

Let  $(S, \leq)$  be a strictly ordered monoid, R be a commutative ring with an identity element and M be an R-module. Let  $R^S = \{f \mid f : S \to R\}$  and

$$R[[S]] = \{ f \in R^S | \text{supp}(f) \text{ is Artinian and narrow} \},$$

where supp $(f) = \{s \in S \mid f(s) \neq 0\}.$ 

For any  $f, g \in R[[S]]$ ,  $\operatorname{supp}(f+g) \subseteq \operatorname{supp}(f) \cup \operatorname{supp}(g)$ ,  $\operatorname{supp}(-f) = \operatorname{supp}(f)$ , and  $\operatorname{supp}(fg) \subseteq \operatorname{supp}(f) + \operatorname{supp}(g)$ . Therefore, under pointwise addition and convolution multiplication defined by

$$(fg)(s) = \sum_{(x,y)\in\chi_S(f,g)} f(x)g(y),$$
 (2.1)

for all  $f, g \in R[[S]]$ , where

$$\chi_s(f, g) = \{(x, y) \in \operatorname{supp}(f) \times \operatorname{supp}(g) | xy = s \}$$

is finite, R[[S]] becomes a ring which is known as generalized power series ring (GPSR).

Next, let 
$$M^S = {\alpha | \alpha : S \to M}$$
 and

$$M[[S]] = {\alpha \in M^S | \operatorname{supp}(\alpha) \text{ is Artinian and narrow}},$$

where  $\operatorname{supp}(\alpha) = \{s \in S \mid \alpha(s) \neq 0\}$ . For any  $\alpha$ ,  $\beta \in M[[S]]$ ,  $\operatorname{supp}(\alpha + \beta) \subseteq \operatorname{supp}(\alpha) \cup \operatorname{supp}(\beta)$ ,  $\operatorname{supp}(-\alpha) = \operatorname{supp}(\beta)$ , and  $\operatorname{supp}(\alpha\beta) \subseteq \operatorname{supp}(\alpha) + \operatorname{supp}(\beta)$ . Therefore, under pointwise addition and scalar multiplication defined by

$$(f\alpha)(s) = \sum_{(x,y)\in\chi_s(f,\alpha)} f(x)\alpha(y), \tag{2.2}$$

for all  $f \in R[[S]]$  and  $\alpha \in M[[S]]$ , where

$$\chi_s(f, \alpha) = \{(x, y) \in \text{supp}(f) \times \text{supp}(\alpha) | xy = s\}$$

is finite, M[[S]] acquires the structure of an R[[S]]-module. Next, this module is called generalized power series module (GPSM).

For any  $r \in R$  and any  $s \in S$ , we associate the maps  $c_r, e_s \in R[[S]]$ , defined by

$$c_r(t) = \begin{cases} 1 & \text{if } t = 1 \\ 0 & \text{if } t \neq 1 \end{cases}$$
 (2.3)

and

$$e_s(t) = \begin{cases} 1 & \text{if } t = s \\ 0 & \text{if } t \neq s. \end{cases}$$
 (2.4)

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For any  $m \in M$  and any  $s \in S$ , we define  $d_m^s(t) \in M[[S]]$  by

$$d_m^s(t) = \begin{cases} m & \text{if } t = s \\ 0 & \text{if } t \neq s. \end{cases}$$
 (2.5)

Then, it is clear that  $r \mapsto c_r$  is a ring embedding of R into R[[S]], and  $s \mapsto e_s$  is a monoid embedding of S into the multiplicative monoid of the ring R[[S]], and also  $m \mapsto d_m^0$  is a module embedding of M into M[[S]].

#### 3. Sufficient Conditions for GPSM M[[S]] to be T[[S]]-Noetherian

In this section we give the sufficient conditions for GPSM M[S] to be T[[S]]-Noetherian module. For any ring R and for some  $n \ge 1$ , we denote  $R \oplus R \oplus \cdots \oplus R$  (n factors), by  $\bigoplus R^{(n)}$ . The necessary and sufficient condition for R-module M to be a finitely generated module is given by the following lemma.

**Lemma 3.1** (See [2, Lemma 3]). *M is finitely generated R-module if and only if it is isomorphic to a quotient of*  $\oplus$   $R^{(n)}$  *for some* n > 0.

For any subset N of an R-module M, we define

$$N[[S]] = \{ \alpha \in M[[S]] | \alpha(s) \in N; \forall s \in S \}.$$

The following lemma shows that N[[S]] is an R[[S]]-submodule of M[[S]].

**Lemma 3.2.** Let M be an R-module and M[S] be an R[S]-module. Then, N[S] is an R[S]-submodule of M[S].

**Proof.** For any  $\alpha$ ,  $\beta \in N[[S]]$  and f,  $g \in R[[S]]$ , we will show that  $\alpha f + \beta g \in N[[S]]$ . In other words, it is enough to show  $(\alpha f + \beta g)(s) \in N$  for every  $s \in S$ . For any  $\alpha \in N[[S]]$ ,  $f \in R[[S]]$ , and for every  $s \in S$ ,  $(\alpha f)(s) = \sum_{uv=s} \alpha(u) f(v)$ . Since N is an R-submodule of M and  $\alpha \in S$ 

T[[S]]-Noetherian Property on Generalized Power Series Modules 5 N[[S]],  $\alpha(u) f(v) \in N$ . Hence,  $(\alpha f)(s) \in N$  for every  $s \in S$ . In similar way, for any  $\beta \in N[[S]]$ ,  $g \in R[[S]]$ , and for every  $s \in S$ , we obtain  $(\beta g)(s) \in N$ . Therefore,  $(\alpha f + \beta g)(s) \in N$  for every  $s \in S$ . So, N[[S]] is an R[[S]]-submodule of M[[S]].

The following proposition shows that a GPSM with coefficients from M/N is equivalent with a module factor of GPSM M[[S]]/N[[S]].

**Proposition 3.3.** Let M be an R-module and M[[S]] be an R[[S]]-module. If N is an R-submodule of M, then  $(M/N)[[S]] \cong M[[S]]/N[[S]]$ .

**Proof.** For any *R*-submodule *N* of *M*, let  $p_N$  be a natural projection. Next, we define a map  $\varphi: M[[S]] \to (M/N)[[S]]$ , by

$$\alpha \mapsto \overline{\alpha} = p_N \circ \alpha$$
,

for every  $\alpha \in M[[S]]$ . It is easy to show that  $supp(\overline{\alpha})$  is Artinian and narrow, which is  $\overline{\alpha} \in (M/N)[[S]]$ .

For any  $\overline{\alpha} \in (M/N)[[S]]$ , there exist  $\alpha \in M[[S]]$ . Then  $\varphi$  is surjective. Therefore,  $\operatorname{Im}(\varphi) = (M/N)[[S]]$ . Next, if  $\varphi(\alpha) = \overline{0}$  for any  $\alpha \in M[[S]]$ , then  $\overline{\alpha} = p_N \circ \alpha = \overline{0}$ . Therefore,  $\alpha(s) \in N$  for every  $s \in S$ . So,  $\operatorname{Ker}(\varphi) = N[[S]]$ . Hence, based on the fundamental isomorphism theorem of modules, we obtain  $(M/N)[[S]] \cong M[[S]]/N[[S]]$ .

The following proposition shows that the GPSR over  $\bigoplus R^{(n)}$  is isomorphic to the direct sum of GPSR  $R[[S]] \bigoplus \cdots \bigoplus R[[S]]$  (*n* factors).

**Proposition 3.4.** Let R be a ring,  $(S, \leq)$  be a strictly ordered monoid, R[[S]] be a GPSR and  $n \geq 1$ . Then  $(\bigoplus R^{(n)})[[S]] \cong \bigoplus (R[[S]])^{(n)}$ .

**Proof.** It is a special case of [2, Proposition 9], by choosing  $R_i = R$  for every i and a monoid homomorphism  $\omega^{(i)}(s) = id_{R_i}$  for every  $s \in S$ .

The sufficient condition for R[[S]]-module M[[S]] to be finitely generated module is given by the following proposition.

**Proposition 3.5.** Let M be an R-module and M[[S]] be an R[[S]]-module. If M is finitely generated, then so is M[[S]].

**Proof.** Based on Lemma 3.1, it is enough to show  $M[[S]] = \bigoplus (R[[S]])^{(n)}/N$ , for some submodule N of  $\bigoplus (R[[S]])^{(n)}$ . Since M is finitely generated, by Lemma 3.1,  $M \cong \bigoplus R^{(n)}/K$ , for some submodule K of  $\bigoplus R^{(n)}$ . Since K is a submodule of  $\bigoplus R^{(n)}$ , based on Lemma 3.2 K[[S]] is a submodule of  $(\bigoplus R^{(n)})[[S]]$ . Furthermore, base on Proposition 3.4, we have K[[S]] is a submodule of  $\bigoplus (R[[S]])^{(n)}$ . Hence, we can choose N = K[[S]].

Now, we will show,  $(\bigoplus R^{(n)}/K)[[S]] \cong \bigoplus (R[[S]])^{(n)}/K[[S]]$ . By using Proposition 3.3, we get

$$(\oplus R^{(n)}/K)[[S]] \cong (\oplus R^{(n)})[[S]]/K[[S]].$$

Furthermore, by using Proposition 3.4, we get  $(\oplus R^{(n)})[[S]] \cong \oplus (R[[S]])^{(n)}$ .

So,  $(\bigoplus R^{(n)}/K)[[S]] \cong (\bigoplus R^{(n)})[[S]]/K[[S]] \cong \bigoplus (R[[S]])^{(n)}/K[[S]]$ . In other words,  $M[[S]] \cong \bigoplus (R[[S]])^{(n)}/N$ , or M[[S]] is finitely generated as an R[[S]] -module.

Next, for any subset *T* of a ring *R*, we define the set

$$T[[S]] = \{ f \in R[[S]] | f(s) \in T; \forall s \in \text{supp}(f) \}.$$

It is clear that  $T[[S]] \subseteq R[[S]]$ . The sufficient conditions of T[[S]] to be a multiplicatively closed subset of GPSR R[[S]] are given by the following lemma.

**Lemma 3.6.** Let R be a ring, T be a multiplicative subset of R,  $(S, \leq)$  be a strictly ordered monoid, and R[[S]] be a GPSR. If T is additively closed, then T[[S]] is a multiplicative subset of R[[S]].

**Proof.** For any  $f, g \in T[[S]]$ , we will show that  $fg \in T[[S]]$ . Based on the convolution multiplication in equation (2.1), for any  $s \in \text{supp}(fg)$  we obtain  $(fg)(s) = \sum_{xy=s} f(x)g(y)$ . Since  $T \subseteq R$  is multiplicatively and additively closed, we have  $\sum_{xy=s} f(x)g(y) \in T$  for every  $s \in \text{supp}(fg)$ . In other words,  $fg \in T[[S]]$ . Thus, T[[S]] is a multiplicatively closed subset of R[[S]].

From equation (2.3), it clear that R is isomorphic to the subring  $\{c_r \mid r \in R\}$  of R[[S]]. Thus, if T is a multiplicative subset of R, then  $C(T) = \{c_t \mid t \in T\}$  is a multiplicative subset of R[[S]]. Then, it is clear that  $T \cong C(T) \subseteq T[[S]]$ .

We recall a multiplicative subset T of a ring R is anti-Archimedean if  $\bigcap_{n\geq 1} t^n RT \neq \emptyset$ , for every  $t\in T$ . The sufficient conditions for R[[S]]-module M[[S]] to be a T[[S]]-Noetherian module are given by the following theorems.

**Theorem 3.7.** Let  $T \subseteq R$  be an additive and multiplicative set with anti-Archimedean property, R be a T-Noetherian ring,  $S = \mathbb{N} \cup \{0\}$  be a strictly ordered monoid with a trivial order  $\leq$ , and M be a finitely generated R-module. Then, R[[S]]-module M[[S]] is T[[S]]-Noetherian.

**Proof.** Since R is T-Noetherian,  $T \subseteq R$  is an anti-Archimedean multiplicative subset of R and  $S = \mathbb{N} \cup \{0\}$  is a strictly ordered monoid with a trivial order  $\leq$ , based on [2, Proposition 9], R[[S]] is T-Noetherian. Next, based on Proposition 3.5, M[[S]] is finitely generated as an R[[S]]-module. Then, based on [3, Lemma 2.14(4)], we get M[[S]] is T-Noetherian.

Furthermore, based on Lemma 3.6., T[[S]] is a multiplicative subset of R[[S]].

Since  $T \subseteq T[[S]]$ , based on [3, Remark 2.11(2)], we have M[[S]] is T[[S]]-Noetherian.

**Theorem 3.8.** Let  $T \subseteq R$  be an additive and multiplicative set with anti-Archimedean property, R be a T-Noetherian ring,  $S = \mathbb{Z}$  be a strictly ordered monoid with a trivial order  $\leq$ , and M be a finitely generated R-module. Then, R[[S]]-module M[[S]] is T[[S]]-Noetherian.

**Proof.** Since R is T-Noetherian,  $T \subseteq R$  is an anti-Archimedean multiplicative subset of R and  $S = \mathbb{Z}$  is a strictly ordered monoid with a trivial order  $\leq$ , based on [3, Proposition 3.4], R[[S]] is T-Noetherian. Next, based on Proposition 3.5, M[[S]] is finitely generated as an R[[S]]-module. Then, based on [3, Lemma 2.14(4)], we get M[[S]] is T-Noetherian. Furthermore, based on Lemma 3.6, T[[S]] is a multiplicative subset of R[[S]]. Since  $T \subseteq T[[S]]$ , based on [3, Remark 2.11 (2)], we have M[[S]] is T[[S]]-Noetherian.

**Theorem 3.9.** Let  $T \subseteq R$  be an additive and multiplicative set with anti-Archimedean property consisting of nonzero divisor, R be a T-Noetherian ring,  $S = \mathbb{N} \cup \{0\}$  be a strictly ordered monoid with a usual order  $\leq$ , and M be a finitely generated R-module. Then, R[[S]]-module M[[S]] is T[[S]]-Noetherian.

**Proof.** Since R is T-Noetherian,  $T \subseteq R$  is an anti-Archimedean multiplicative subset of R consisting of nonzero divisor and  $S = \mathbb{N} \cup \{0\}$  is a strictly ordered monoid with a usual order  $\leq$ , based on [2, Proposition 10], R[[S]] is T-Noetherian. Next, based on Proposition 3.5, M[[S]] is finitely generated as an R[[S]]-module. Then, based on [3, Lemma 2.14(4)], we get M[[S]] is T-Noetherian. Furthermore, based on Lemma 3.6, T[[S]] is a

T[[S]]-Noetherian Property on Generalized Power Series Modules 9 multiplicative subset of R[[S]]. Since  $T \subseteq T[[S]]$ , based on [3, Remark 2.11 (2)], we have M[[S]] is T[[S]]-Noetherian.

**Theorem 3.10.** Let  $T \subseteq R$  be an additive and multiplicative set with anti-Archimedean property consisting of nonzero divisor, R be a T-Noetherian ring,  $S = \mathbb{Z}$  be a strictly ordered monoid with a usual order  $\leq$ , and M be a finitely generated R-module. Then, R[[S]]-module M[[S]] is T[[S]]-Noetherian.

**Proof.** Since R is T-Noetherian,  $T \subseteq R$  is an anti-Archimedean multiplicative subset of R consisting of nonzero divisor and  $S = \mathbb{Z}$  is a strictly ordered monoid with a usual order  $\leq$ , based on [5], Theorem 3.1], R[[S]] is T-Noetherian. Next, based on Proposition 3.5, M[[S]] is finitely generated as an R[[S]]-module. Then, based on [3], Lemma 2.14(4)], we get M[[S]] is T-Noetherian. Furthermore, based on Lemma 3.6, T[[S]] is a multiplicative subset of R[[S]]. Since  $T \subseteq T[[S]]$ , based on [3], Remark 2.11(2)], we have M[[S]] is T[[S]]-Noetherian.

**Theorem 3.11.** Let  $T \subseteq R$  be an additive and multiplicative set with anti-Archimedean property consisting of nonzero divisor, R be a T-Noetherian ring, S be a finitely generated strictly ordered monoid with a positive order  $\leq$ , and M be a finitely generated R-module. Then, R[[S]]-module M[[S]] is T[[S]]-Noetherian.

**Proof.** Since R is T-Noetherian,  $T \subseteq R$  is an anti-Archimedean multiplicative subset of R consisting of nonzero divisor and S is a finitely generated strictly ordered monoid with a positive order  $\leq$ , based on [5, Theorem 2.3], R[[S]] is T-Noetherian. Next, based on Proposition 3.5, M[[S]] is a finitely generated as an R[[S]]-module. Then, based on [3, Lemma 2.14(4)], we get M[[S]] is T-Noetherian. Furthermore, based on Lemma 3.6, T[[S]] is a multiplicative subset of R[[S]]. Since  $T \subseteq T[[S]]$ , based on [3, Remark 2.11(2)], we have M[[S]] is T[[S]]-Noetherian.

**Theorem 3.12.** Let R be a ring,  $T \subseteq R$  be a multiplicative set,  $(S, \leq)$  be a strictly ordered monoid, and M be an R-module. If R is Noetherian, T is additively closed,  $(S, \leq)$  is narrow, S is cancelative and torsion-free,  $\exists s_1, ..., s_n \in S \backslash G(S)$  such that  $S = \langle s_1, ..., s_n \rangle + G(S)$ , and M is finitely generated, then R[[S]]-module M[[S]] is T[[S]]-Noetherian.

**Proof.** Based on [7, Theorem 5.5], R[[S]] is Noetherian. Therefore, by the definition, R[[S]] is T-Noetherian for any multiplicative subset T of R. Next, based on Proposition 3.5, M[[S]] is finitely generated as an R[[S]]-module. Then, based on [3, Lemma 2.14(4)], we get M[[S]] is T-Noetherian. Furthermore, based on Lemma 3.6, T[[S]] is a multiplicative subset of R[[S]]. Since  $T \subseteq T[[S]]$ , based on [3, Remark 2.11(2)], we have M[[S]] is T[[S]]-Noetherian.

**Theorem 3.13.** Let R be a ring,  $T \subseteq R$  be a multiplicative set,  $(S, \leq)$  be a strictly ordered monoid, and M be an R-module. If T is additively closed,  $(S, \leq)$  is narrow, S is cancelative and torsion-free,  $\exists s_1, ..., s_n \in S \backslash G(S)$  such that  $S = \langle s_1, ..., s_n \rangle + G(S)$ , M is Noetherian, and  $N = \{x \in M \mid Rx \subseteq N\}$  for every submodule N of M, then R[[S]]-module M[[S]] is T[[S]]-Noetherian.

**Proof.** Based on [4, Theorem 4.6], M[[S]] is Noetherian as an R[[S]]-module. Therefore, by the definition, M[[S]] is T-Noetherian for any multiplicative subset T of R. Furthermore, based on Lemma 3.6, T[[S]] is a multiplicative subset of R[[S]]. Since  $T \subseteq T[[S]]$ , based on [3, Remark 2.11(2)], we have M[[S]] is T[[S]]-Noetherian.

#### 4. Conclusions

In this section, we give the conclusion of the main results of this paper. These conclusions, we present in the following table:

**Table 1.** Sufficient conditions for GPSM M[[S]] to be T[[S]]-Noetherian

Assumptions					
Ring R	Multiplicatively closed set $T \subseteq R$	Strictly order monoid $(S, \leq)$	R-module M	Theorem	
T-Noetherian	■ anti- Archimedean ■ additively closed	<ul> <li>S = N ∪ {0}</li> <li>trivial ≤</li> </ul>	finitely generated	3.7	
		<ul> <li>S = Z</li> <li>trivial ≤</li> </ul>		3.8	
	<ul> <li>anti-         Archimedean consisting of nonzero divisor     </li> <li>additively</li> <li>closed</li> </ul>	■ S = N U {0} ■ usual ≤		3.9	
		$S = \mathbb{Z}$ $usual \leq$		3.10	
		■ f.g. S ■ positive ≤		3.11	
Noetherian		<ul> <li>(S, ≤) is narrow</li> <li>S is cancelative and torsion-free</li> <li>∃s<sub>1</sub>,, s<sub>n</sub> ∈ S\G(S)</li> <li>s.t. S = ⟨s<sub>1</sub>,, s<sub>n</sub>⟩</li> <li>+G(S)</li> </ul>		3.12	
Any	Additively closed	■ $(S, \leq)$ is narrow ■ $S$ is cancelative and torsion-free ■ $\exists s_1,, s_n \in S \setminus G(S)$ , s.t. $S = \langle s_1,, s_n \rangle$ + G(S)	■ $M$ is Noetherian ■ $N = \{x \in M \mid Rx \subseteq N\},$ for every $N \leq M$	3.13	

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